



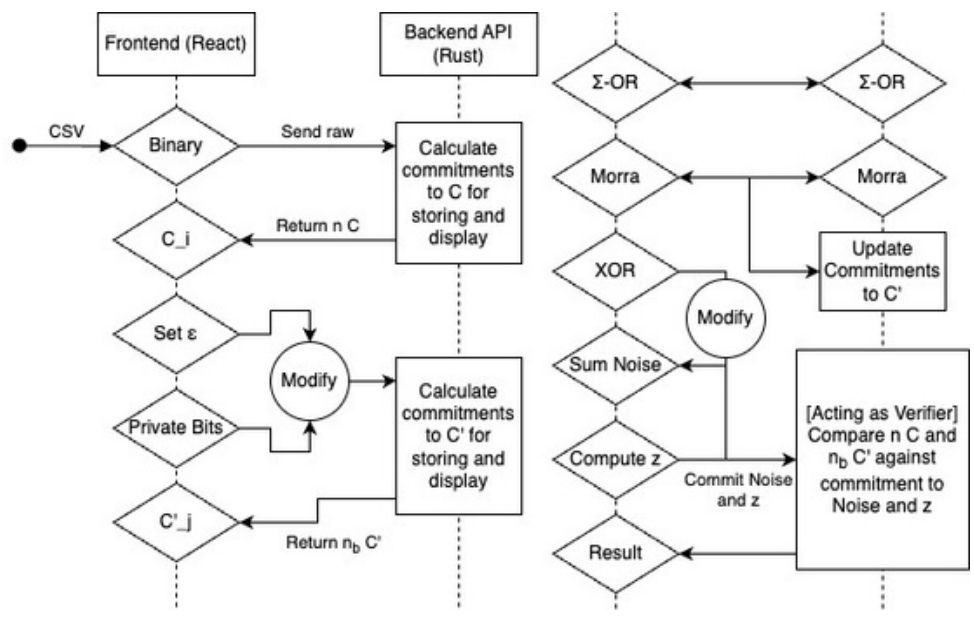
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Website Demo

The React frontend, written in TypeScript, guides users step-by-step through the protocol. After uploading a CSV file and choosing a column and threshold, the interface prompts users to commit their data values; it then invites them to play the Morra game against the server to generate provably fair random bits. As each commitment or proof is submitted, the site visualizes the underlying zero-knowledge transcript, and if a user attempts to “cheat” by altering a bit or misreporting randomness, the Rust verifier immediately flags the inconsistency. The UI then informs the user that the check failed, teaching users why zero-knowledge proofs enforce both privacy and correctness. All code is open-source on GitHub (github.com/mwagner6/zkdp-exponential), and future updates will extend the site to support biased-binomial and randomized-response mechanisms, port critical libraries to WebAssembly, and integrate with the OpenDP ecosystem for seamless adoption of verifiable DP.

Website API Flow

Our final contribution is a **zero-knowledge protocol for randomized response that can potentially avoid homomorphic commitments**. Instead, the prover generates k private fair coins, which are XORed with k public fair coins from the Morra oracle to create a uniform random number U in the range $\{0, \dots, 2^k - 1\}$. The prover then flips their bit x with probability $p = m / 2^k$ by computing the output $o = x \text{ XOR } [U < m]$. All values involved are committed to using standard one-way commitments, and the prover provides a zero-knowledge proof that the output was computed correctly from the committed values. This approach significantly reduces cryptographic overhead and removes the need for group structure, relying only on the existence of one-way functions. While the current design is limited to binary outputs and flip probabilities where p is a rational number with denominator a power of two, it demonstrates that verifiable differential privacy can be achieved under minimal cryptographic assumptions.



Algorithm 3: Alternative Randomised response with flip probability p

Input: A rational probability $p = m/2^k$, such that m and k are integers; client's private data $x \in \{0, 1\}$

Output: A single biased bit r revealed to the verifier

- 1: Prover commits c_1, c_2, \dots, c_k and gives a Σ -OR proof each commitment is a bit.
- 2: Generate $b_1, \dots, b_k \leftarrow \mathcal{M}_{\text{MORRA}}$.
- 3: Prover computes $d_i := v_i \oplus b_i$ and $U = \sum_{i=1}^k d_i 2^{i-1}$.
- 4: Output $o := x \oplus \lfloor U < m \rfloor$.
- 5: Prover proves in zero knowledge that (i) Line 1 was honest and (ii) Line 4 holds for the committed values.

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