

CS208: Applied Privacy for Data Science Programming Frameworks

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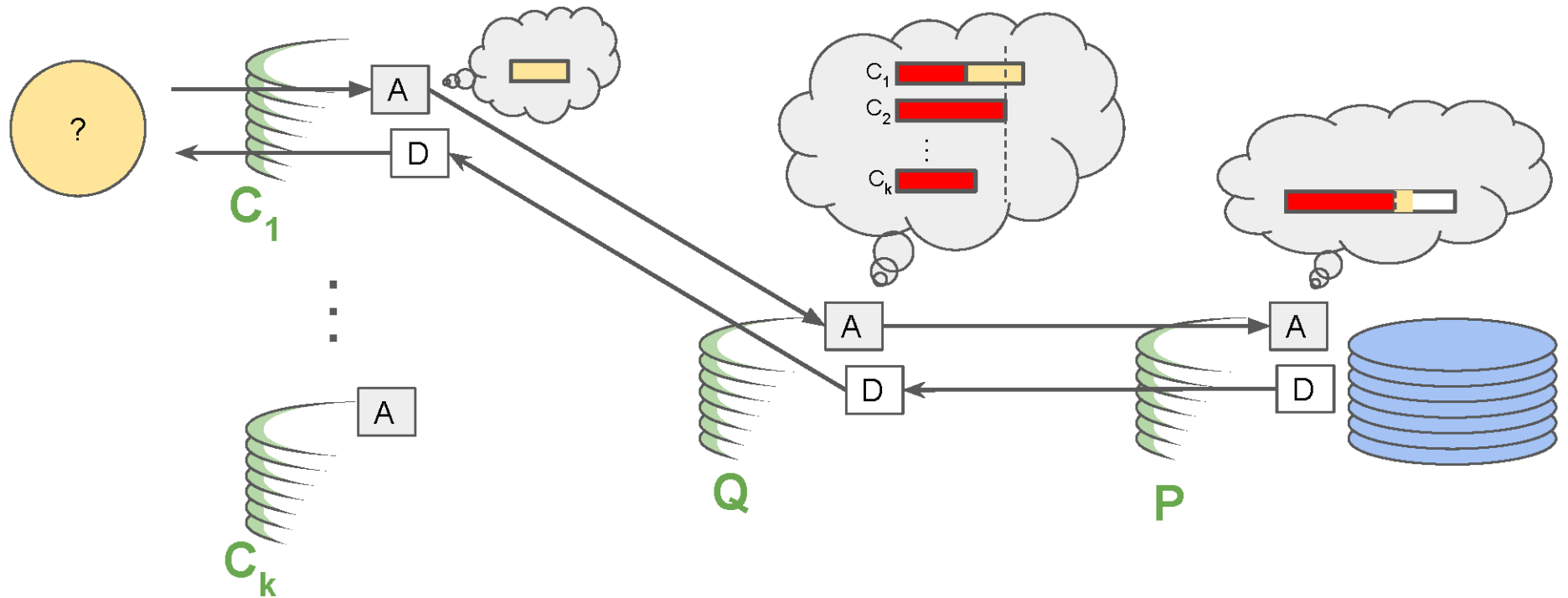
Programming Frameworks for DP

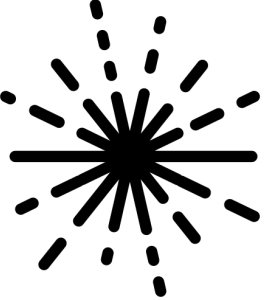
Goal: make it easier for a data custodian or analyst to **write programs** that are DP, and be **confident** that they actually are DP.

Common approach (starting with PinQ [McSherry '09]):

- **(Small) set of trusted DP subroutines:** (Lap, Geo, ExpMech, ...) only channel for info to flow from dataset to rest of program.
- **Track privacy budget consumption:** using composition of DP, with either a runtime monitor or static analysis.
- **Allow “stable” data transformations:** (recursively) track impact on privacy consumption.

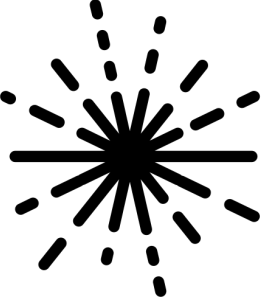
Hierarchical Interactivity in PinQ





OpenDP Programming Framework

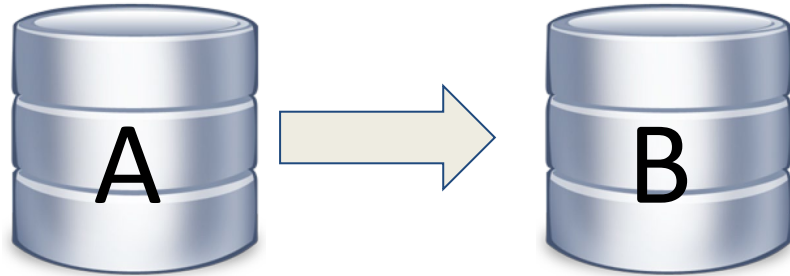
- Generality in privacy definitions & algorithms
 - Pure DP, approximate DP, concentrated DP, f-DP, etc.
 - Node-level privacy in graphs, user-level privacy in streams, etc.
- Generality in privacy calculus
 - Composition, amplification by subsampling, group privacy, etc.
- Safe extensions of framework with vetted contributions
 - Clear spec for each component's privacy-relevant properties
- Interactive DP algorithms as first-class citizens
 - Adaptive composition, sparse vector, etc.
 - Still in implementation!
- Implementation in Rust w/Python bindings



Transformations and Measurements

Transformations:

Function from data(sets) to data(sets).

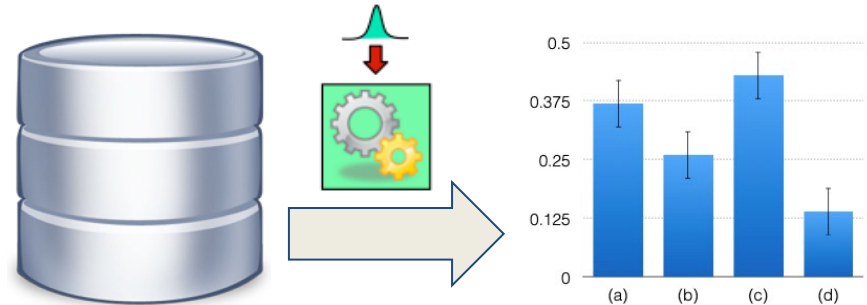


Transformation Attributes

- Input domain
- Input metric
- Output domain
- Output metric
- Function
- Stability relation

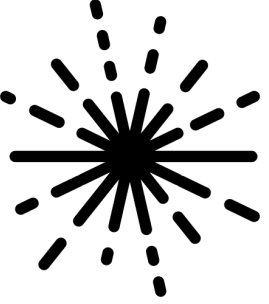
Measurements:

Randomized functions from data(sets) to outputs.

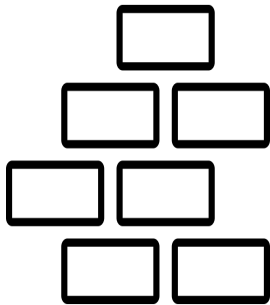


Measurement Attributes

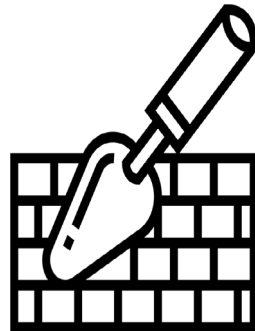
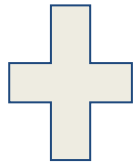
- Input domain
- Input metric
- Output measure
- Function
- Privacy relation



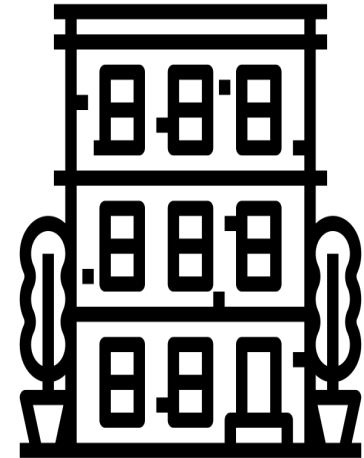
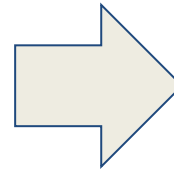
Combinators: Chaining, Composition and Post-processing



Measurements
&
Transformations

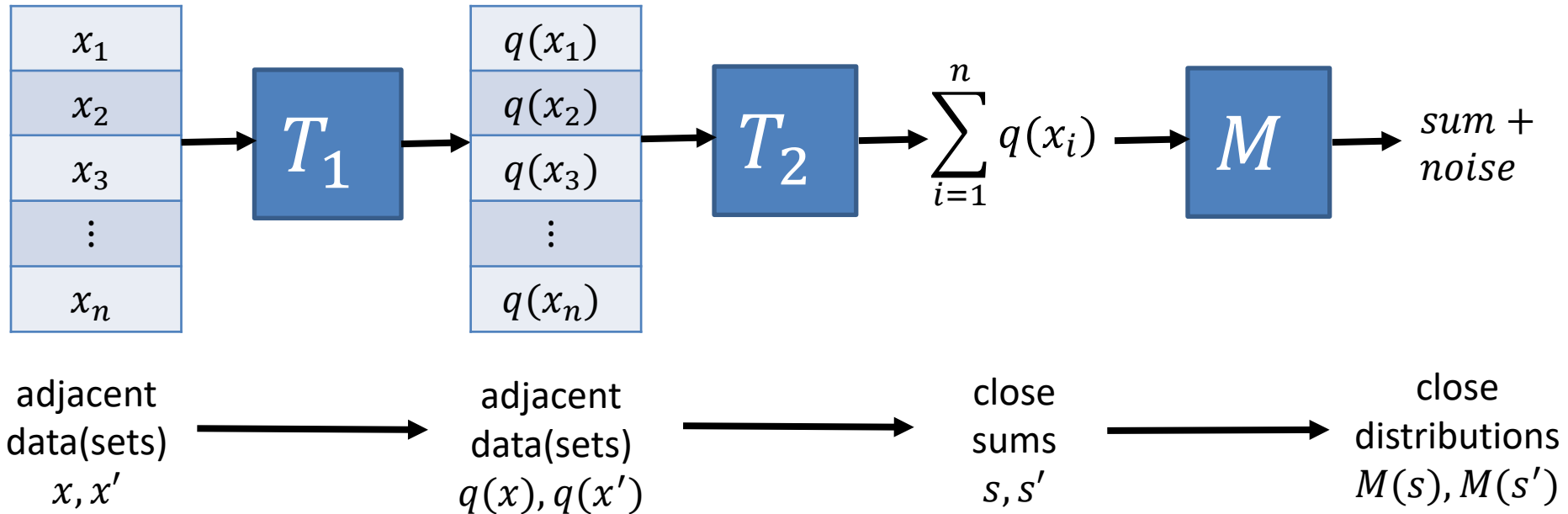


Combinators,
e.g. Chaining,
Composition,
Post-processing

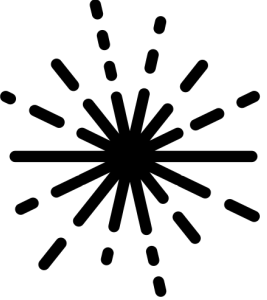


Complex DP
programs

Chaining Transformations & Measurements



The result is a new measurement $M' = T_1 \gg T_2 \gg M$



Privacy calculus: privacy and stability relations

To implement a **privacy calculus** based on the idea of **stability** we have:

- **privacy maps** in measurements to capture several notions of privacy. E.g. DP, approx. DP, Renyi DP, zCDP, f-DP.
- **stability maps** in transformations to capture general aggregate operations. E.g. bounded joins.
- **combination of these maps** by means of combinators such as chaining and composition.

$d_{\text{out}} = \text{map}(d_{\text{in}})$ should imply:
if two inputs are “ d_{in} -close”,
then the corresponding outputs (or
distributions) are “ d_{out} -close”.

Measurement attributes

- Input domain
- Input metric
- **Output measure**
- Function
- **Privacy map**

Transformation attributes

- Input domain
- Input metric
- Output domain
- Output metric
- Function
- **Stability map**

Other Issues in Programming DP

- **Multi-relational databases**
 - Need to define input metric/adjacency carefully
 - Standard joins have unbounded stability constant, so need to truncate results or use “local sensitivity” approximations.
- **Side-channel attacks**
 - Info can be leaked through timing, approx. of real numbers, global state, exceptions, etc.
 - Constrain language & implementation to match model better.
- **Verifying DP building blocks or more complex DP algs**
 - Specialized programming languages.
 - Annotate programs with types to assist automated verification of DP.
 - Tradeoff between usability and expressiveness.
 - Now can even synthesize DP algorithms from examples!
- **Guidance on Accuracy & Privacy Budgeting**
 - Next time!
- **Choice of Programming Model (e.g. SQL vs. MapReduce vs. R)**
- **Machine Learning Frameworks**
 - Main ones are Opacus, Jax-Privacy, TensorFlow-Privacy

Takeaways

- Should not build DP applications from scratch, better to use an existing framework.
- We'll illustrate with OpenDP because we
 - Are most familiar with OpenDP
 - Hope that some of you become OpenDP contributors
- But feel free to use any existing tools out there that are a good fit for your project!